

Parameterisation of multi-map from Internet traffic traces

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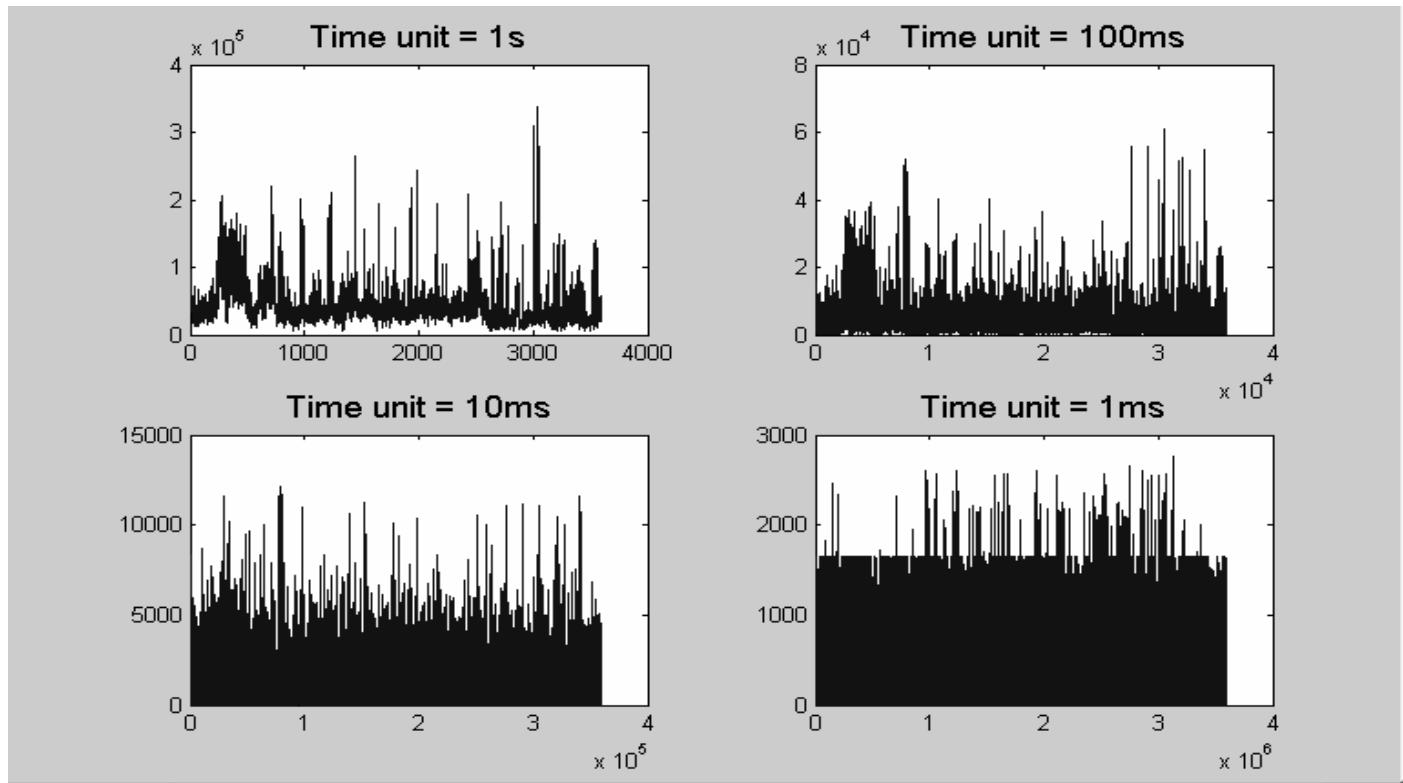
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Presentation Overview

- ❖ Observation of Internet traffic analysis
 - ❖ Observed scalings
- ❖ Multi-map as a traffic model
 - ❖ Structures and equations
 - ❖ Parameters of the map
- ❖ Trace based parameterisation of the multi-map
 - ❖ step by step analysis
- ❖ Comparison of real versus synthetic traffic analysis
 - ❖ R/S scaling comparison, load and variance analysis
- ❖ Future directions
 - ❖ More trace analysis
 - ❖ Model use in network analysis

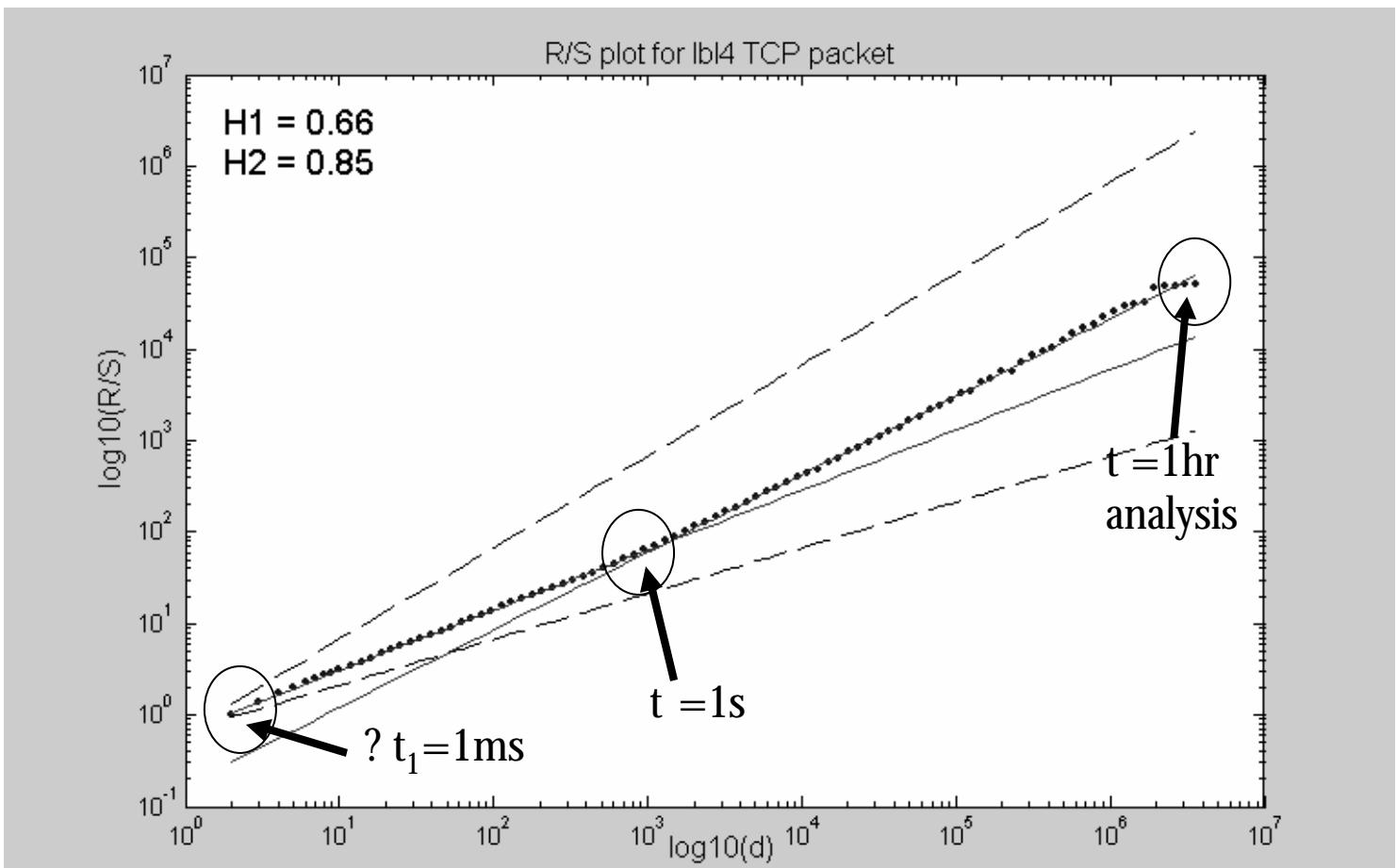
Traffic trace analysis

- ❖ TCP traffic traces from WAN at Berkeley Labs
 - ❖ An hourly trace (lbl-4)
 - ❖ 1.3 million packets in the trace

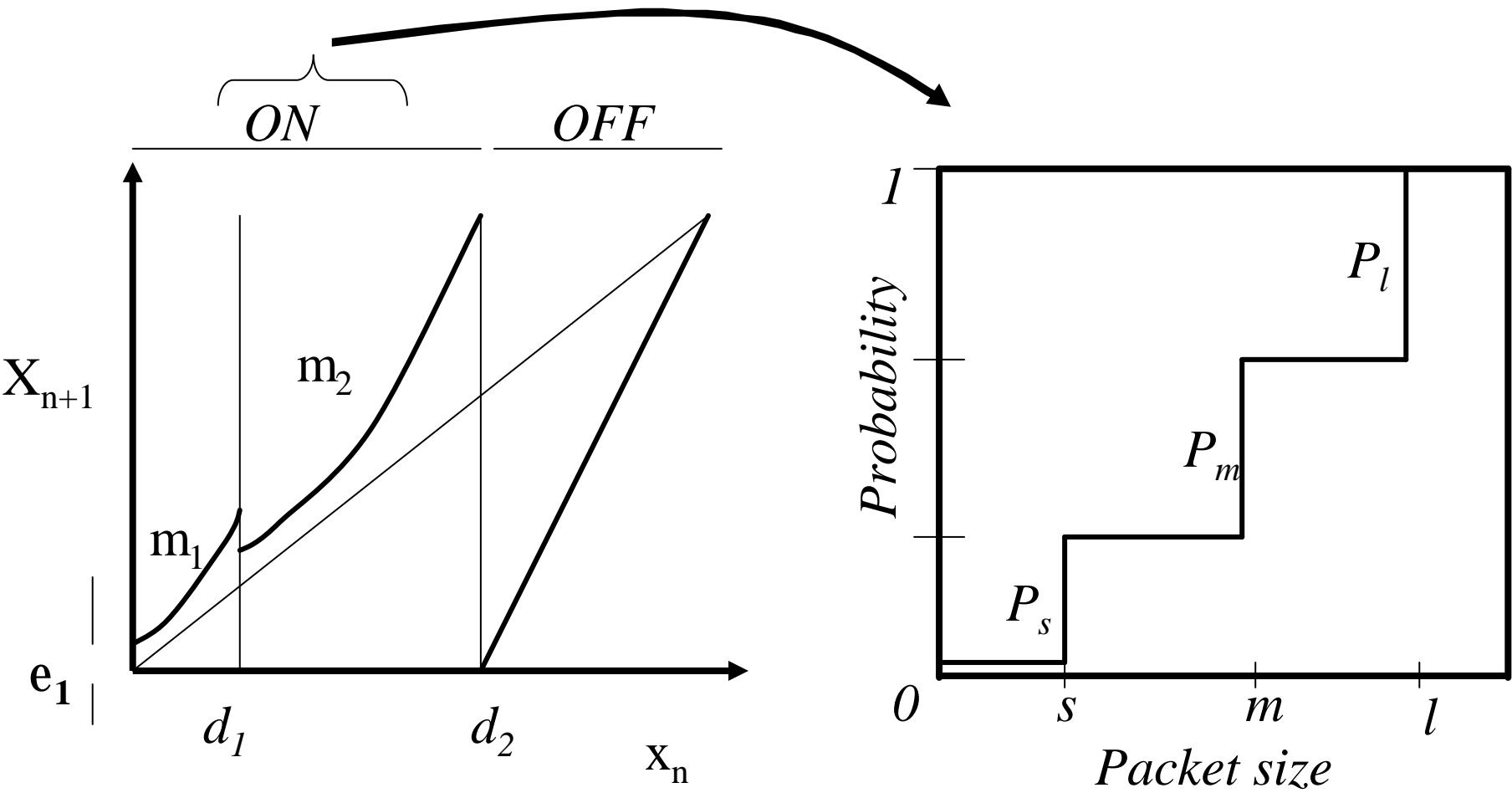


Scaling of traffic traces

- ❖ R/S analysis showed two scaling ranges
 - ❖ Two Hurst parameters with cross over point at around 1s



Structure of multi-map model



Equations of multi-map

❖ Hidden dynamical layer

$$x_{n+1} = F(x_n) = \begin{cases} F_1(x_n) &= e_1 + x_n + \frac{1 - e_1 - d_2}{d_2^{m_1}} x_n^{m_1} & 0 < x_n < d_1 \\ F_2(x_n) &= e_2 + x_n + \frac{1 - e_2 - d_2}{d_2^{m_2}} x_n^{m_2} & d_1 \leq x_n < d_2 \\ F_3(x_n) &= x_n - d_2 \frac{1 - x_n}{1 - d_2} & d_2 \leq x_n < 1 \end{cases}$$

❖ where parameters $x_n \in (0,1)$ $m_i \in (1,2)$ $d_i \in (0,1)$

❖ Visible dynamical layer

$$y(x_n) = \begin{cases} 1 & 0 < x_n < d_2, \\ 0 & d_2 \leq x_n < 1, \end{cases} \quad \begin{array}{l} ON \,(packet) \\ OFF \,(no \, packet) \end{array}$$

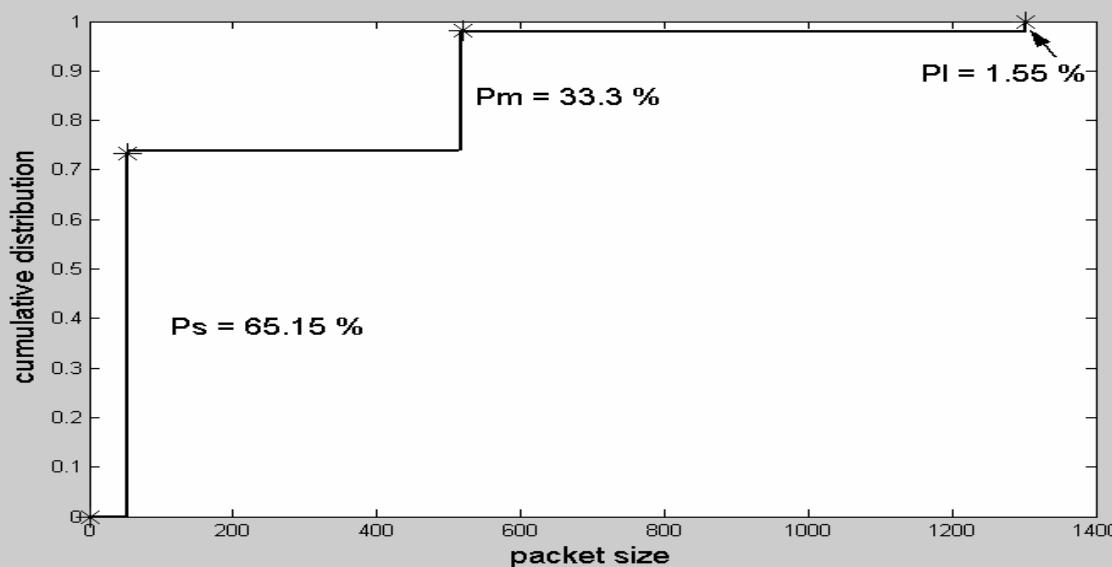
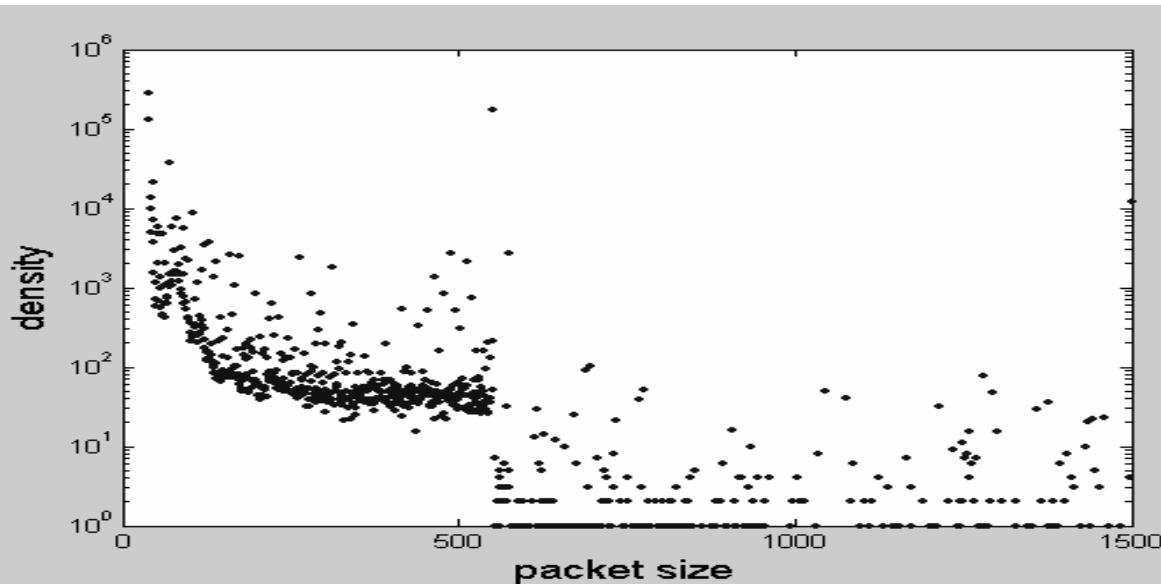
Parameterisation of the multi-map

- ❖ Packet size distribution analysis
 - ❖ Packet sizes - s, m, l , & corresponding - P_s, P_m, P_l
- ❖ Time scale and load analysis
 - ❖ $d_2, ? t_2$
- ❖ Multi scaling analysis
 - ❖ m_1, m_2, e, d_1

Distribution analysis

- ❖ Packet size analysis based on Imix Internet packet mixture [*Journal of Internet test*]
 - ❖ Result of 342 million packet analysis at NLANR
 - ❖ Accurate correlation when compared to realistic Internet traffic
 - ❖ Tri-modal distribution analysis from traces
 - ❖ Output - three mean packet sizes and their distribution
 - ❖ Small, medium and large sizes and respective probabilities

Distribution analysis (contd.)

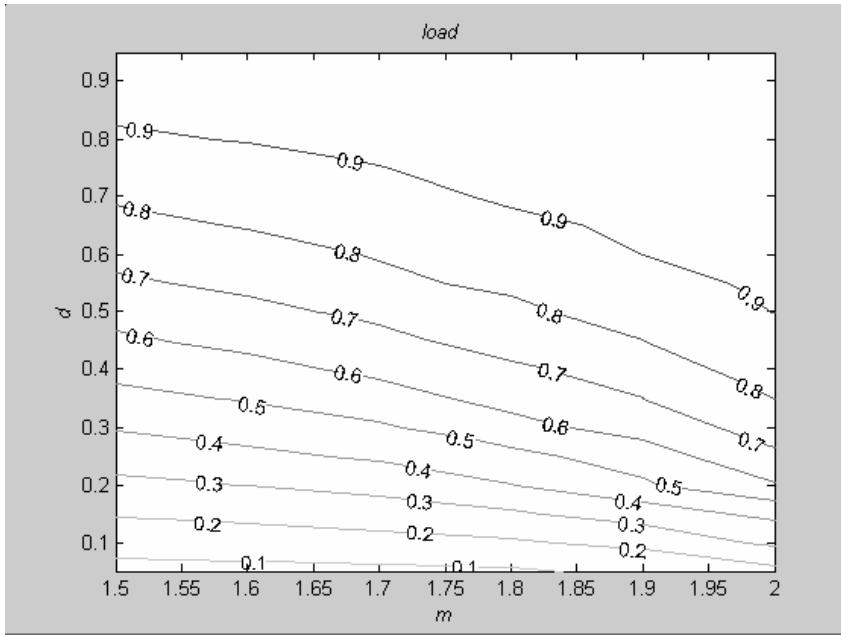


Time scale and load analysis

- ❖ Variance and load calculated for each trace with regards to Δt_1
 - ❖ smallest time scale unit the trace analysed at
- ❖ Respective analysis of iteration time
 - ❖ $\Delta t_2 = P_l/C$
 - ❖ where P_l is max packet size and C is link rate
 - ❖ Hence one iteration corresponds to Δt_2
- ❖ Scaling comparison achieved with equal time units

Time scale and load analysis – parameter d_2

- ❖ Proportion of time increments that have a packet and hence the load, relates to parameter d_2
- ❖ Equivalence to single intermittency map in its structure
 - ❖ Based on look up table of parameters d , m and *load*



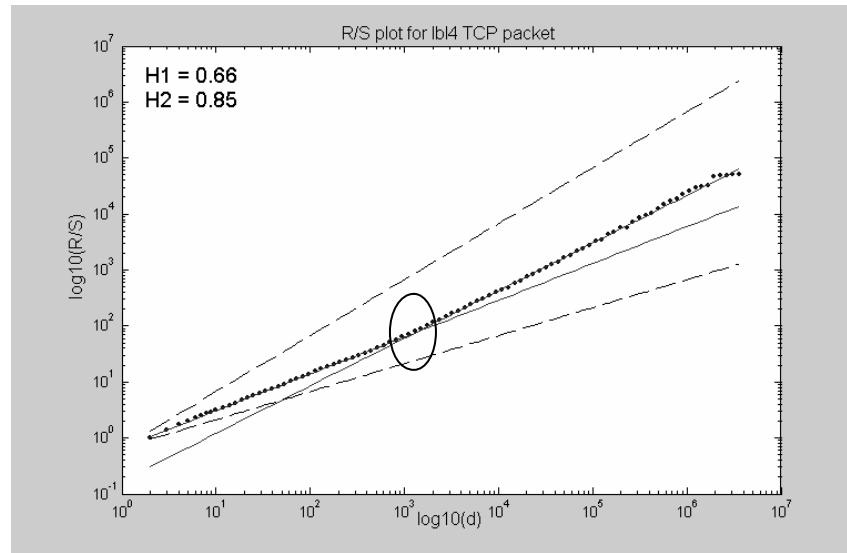
- 11 ❖ Output – parameter d_2 for specific load and m_2

Time scale and load analysis – constraints on parameter d_2

- ❖ Constraints on d_2 [Samuel] leads to changes in parameters
 - ❖ If d_2 lies outside regions 0.1 to 0.9
 - ❖ H value is lower than expected
 - ❖ Hence keep d_2 within the region
 - ❖ Results in changes in proportion of time increments that have a packet
 - ❖ Leads to change in Δt_2 – iteration time unit

Multi scaling analysis – H test

- ❖ Hurst parameter using R/S analysis
 - ❖ Advantage of showing distinctive scaling regions



- ❖ Output – two H values with cross over point
 - ❖ $H_1, H_2, t = n_t * ? t_1$

Multi scaling analysis – Parameters m_1 and m_2

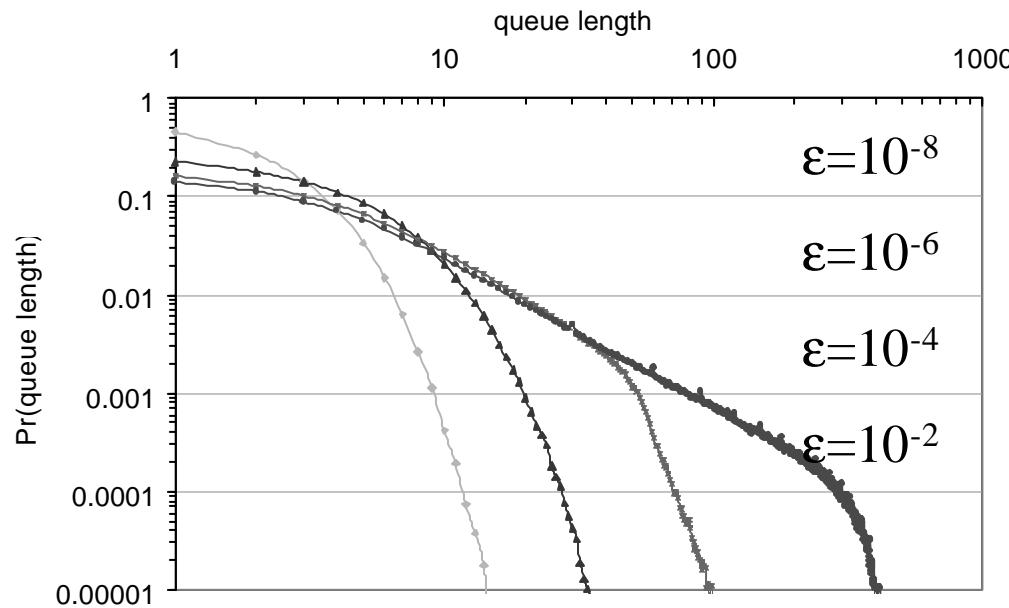
- ❖ The m parameters are directly linked to the Hurst parameters [Mondragon]
- ❖ Equation of m from H parameters

$$H = \left(\frac{3m - 4}{2m - 2} \right)$$
$$\Rightarrow m = \left(\frac{4 - 2H}{3 - 2H} \right)$$

- ❖ Output m_1 and m_2

Multi scaling analysis – Parameter e

- ❖ e parameter allows effective control of LRD
 - ❖ cut-off point in case of single intermittency map
 - ❖ Queue analysis result



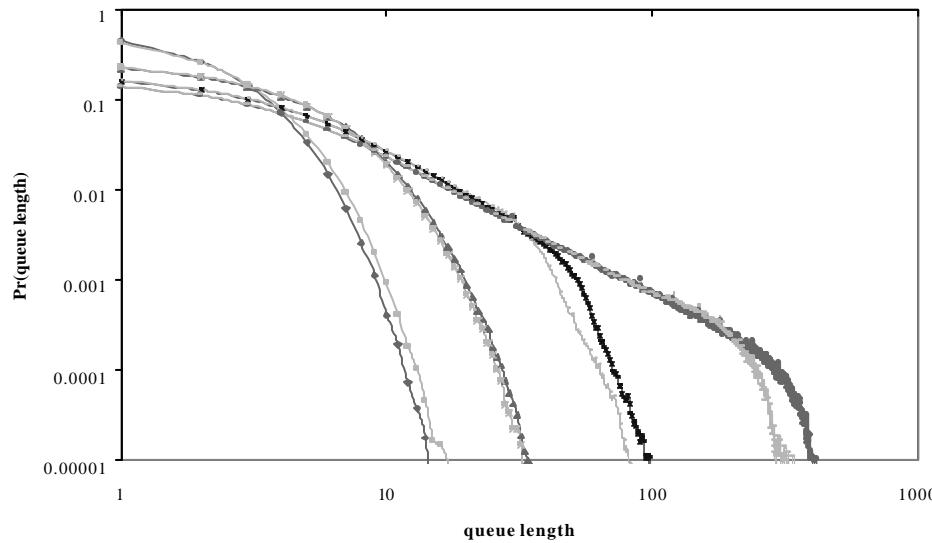
- ❖ Output e versus cross-over point

Multi scaling analysis – Parameter d_1

- ❖ Parameter d_1

$$d_1 = d_2 \left(\frac{e}{1-d_2} \right)^{\frac{1}{m_2}}$$

- ❖ Controls the cross over point
- ❖ Equivalence achieved with single intermittency map



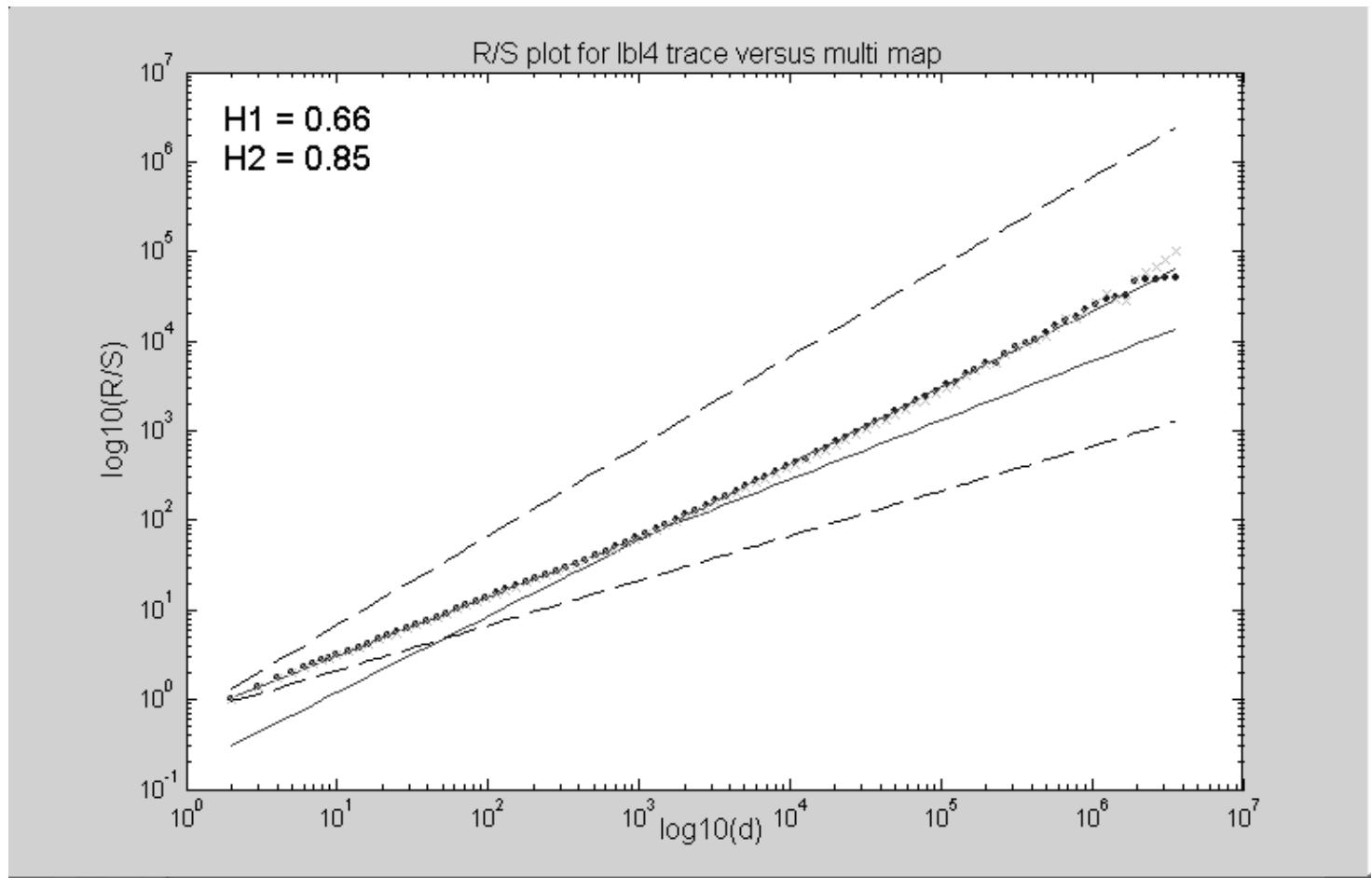
Parameter value results –lbl4

- ❖ Packet size distribution analysis
 - ❖ Packet sizes – $s = 45 \text{ bytes}$, $m = 520 \text{ bytes}$, $l = 1451 \text{ bytes}$,
 - ❖ $P_s = 0.6515$, $P_m = 0.333$, $P_l = 0.0155$
- ❖ Time scale and load analysis
 - ❖ $d_2 = 0.1$, ? $t_2 = 500\mu\text{s}$
- ❖ Multi scaling analysis
 - ❖ $m_1 = 1.8$, $m_2 = 1.6$, $e = 1*10^6$, $d_1 = 1.9*10^{-5}$

Comparison of real versus synthetic traffic

❖ Mean load	
❖ Trace	Multi-map
❖ 330 bit/s	293 bits/s
❖ 0.2397 pps	0.232 pps
❖ Variance	
❖ Trace	Multi-map
❖ 167.8 bit/s	137 bit/s
❖ 0.527 pps	0.5 pps
❖ H parameter	
❖ Trace	Multi-map
❖ 0.66, 0.85	0.65, 0.82

Comparison of real versus synthetic traffic from multi map



Future Directions

- ❖ More trace analysis
 - ❖ York trace
- ❖ Use of traces in network analysis
 - ❖ Advantages of multi-map
 - ❖ Parsimonious, effective parameterisation, fast
 - ❖ Multi service complex traffic scenarios
 - ❖ Traffic generation for different classes of traffic
 - ❖ Performance analysis